

DESIGN OF BACKGEAR MECHANISM IN LATHE

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Abstract

The objective of this project is to determine the design procedure involved in designing back gear mechanisms in lathe. It also gives detail about back gear mechanisms, its layout, its function and its design calculations. Design procedure include the design of hollow spindle, lay shaft, belt drive, gears and bearings. Calculations are made and compared with allowable stresses and allowable dimensions. This ensures a safe design for back gear mechanism's design data book is used for design calculation.

Keywords:

1. Introduction

1.1 Back gear mechanisms

As its name implies, "back gear" is a gear mounted at the back of the headstock that allows the chuck to rotate slowly with greatly-increased turning power. For a novice the ability to run a workpiece slowly might seem unnecessary, but a large-diameter casting, fastened to the faceplate and run at 200 r.p.m would have a linear speed at its outer edge beyond the turning capacity of a small lathe. By engaging back gear, and so reducing r.p.m. but increasing torque, even the largest faceplate-mounted jobs can be turned successfully.

1.2. Layout diagram

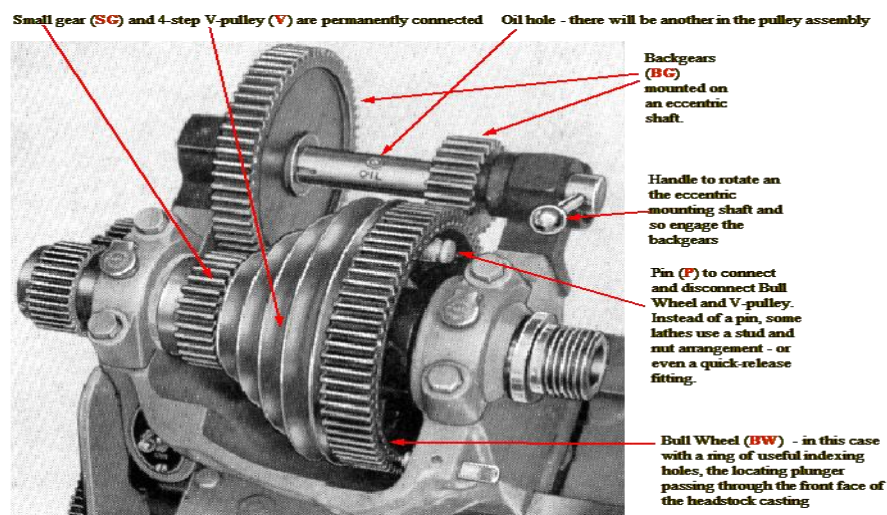


Fig1: This is layout diagram of 1934 Atlas lathe which has the 4-step V-pulley (V) with a small gear (SG) permanently attached to its smaller end. The entire length of V-pulley and gear are bushed - and able to rotate freely on the headstock spindle.

1.3. Working of back gear mechanism

In normal use the V-pulley is rotated by the drive belt and the spindle turned through the action of the pin driving the Bull Wheel and hence the spindle to which it is connected.

To engage back gear the lathe is stopped, the pin (**P**) withdrawn leaving the pulley and small gear free to rotate and the Back gear (**BG**) rotated on its eccentric shaft to bring it into mesh with the other gears. On starting the lathe action is now as follows: the pulley is rotated by the drive belt with the small gear (**SG**) on the V-pulley (**V**) driving the larger of the two rear-mounted back gears - which in turn causes the smaller gear at the other end of its shaft to rotate. This smaller gear drives the Bull Wheel (**B**), and hence the spindle at a much lower speed (normally in the order of a 8 : 1 reduction) but with greatly increased torque.

2. Design calculation

2.1 Requirements.

Initial requirement for design calculation of drive arrangement are taken as follows,

The lifting is provided by a 7 kW two speed electrical motor running at 720 rpm. The power is transmitted to the rope drum through a belt drive and a two stage spur gear reduction unit. The speed reduction in the belt drive is 2, while the overall speed reduction in the spur gear reducer is 16.

Design following

1. Design of belt drive
2. Design of gear
3. Design of main hollow spindle

2.2 Design of belt drive

Type of belt drive used in drive arrangement for a tiller crane is V Belt drive.

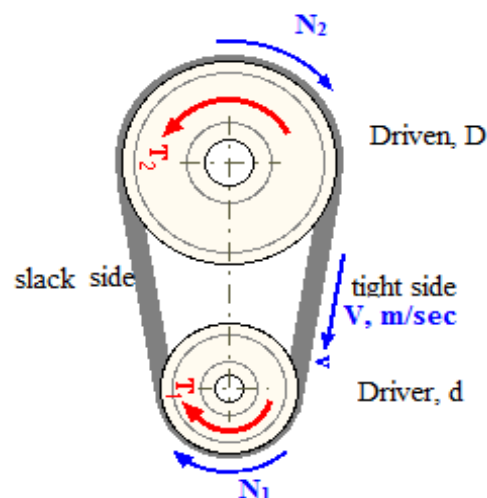


Fig:2.2.1 Pulley Arrangement

2.2.1 Known Parameters

| | |
|-------------------------------------------------------|--------------------------------------------------------------------------------|
| Center to center distance of driver and driven pulley | $C = 250 \text{ mm}$ |
| Power | $P = 3.5 \text{ HP}$ $= 3.5 \times 736 \text{ KW}$ $P = 2576 \text{ KW}$ |
| Speed of input shaft (from motor) | $N_1 = 550 \text{ rpm}$ |
| Diameter of input shaft | $d_1 = 300 \text{ mm}$ |
| Diameter of driven shaft | $d_2 = 550 \text{ rpm}$ |
| Tension on tight side of belt | $T_1 = 200 \text{ N}$ $T_1/T_2 = 3$ |
| Ratio of tension between tight sides to slag side | $[\sigma] = 40 \text{ MPa}$ |
| Safe stress | |

2.2.2 Selection of belt section

From design data book page no. 7.58 *B Section* is selected for the given power of 2.5 KW

- Nominal top width $w = 17 \text{ mm}$
- Nominal thickness $T = 11 \text{ mm}$

Speed of driven pulley (N_2)

$$\frac{d_2}{d_1} = \frac{N_1}{N_2}$$

$$\frac{550}{300} = \frac{550}{N_2}$$

$$N_2 = 300 \text{ rpm}$$

Therefore speed of driven pulley is 300rpm

Nominal pitch length of belt

From design data book 7.61

$$L = 2C + \pi (d_1 + d_2) / 2 + (d_2 - d_1)^2 / 4C$$

$$= (2 \times 250) + \pi (300 + 550) / 2 + (550 - 300)^2 / (4 \times 250)$$

$$L = 1948 \text{ mm}$$

Arc of contact angle

$$\theta = 180 - 60 \left(\frac{d_2 - d_1}{4C} \right)$$

$$\theta = 165$$

Maximum Power Capacity Of Belt

$$\text{Maximum power capacity} = (0.79 \times S^{-0.09} - 50.8/d_e - 1.32 \times 10^{-4} S^2) S$$

S - Belt speed in m/s

d_e - Equivalent pitch diameter in mm

- Belt speed $S = \pi d_1 N_1 / 60$

$$= \pi \times 300 \times 550 / 60$$

$$S = 8.640 \text{ m/s}$$

Equivalent pitch diameter $d_e = d_p \times F_b$

- pitch dia of smaller pulley (d_p) = 300 mm

- F_b for $p/d (= 1.833) = 1.13$

$$d_e = 1.13 \times 300$$

$$d_e = 339 \text{ mm}$$

$$\begin{aligned} \text{Maximum power capacity} &= (0.79 \times S^{-0.09} - 50.8/d_e - 1.32 \times 10^{-4} S^2) S \\ &= 4.32 \text{ KW} \end{aligned}$$

Determination of number of belts

$$n_b = (P \times F_a) / (KW \times F_c \times F_d)$$

Service factor, $F_a = 1.1$ (up to 10 hrs light duty per day, from design data book page no 7.67)

Length correction factor, $F_c = 0.97$ (from design data book page no 7.68)

Correction factor for arc of contact, $F_d = 0.79$ (from design data book page no 7.68)

$$n_b = (2.5 \times 1.1) / (4.32 \times 0.97 \times 0.79)$$

$$n_b = 0.83 = 1 \text{ belt}$$

Modified center distance or actual center distance

$$\begin{aligned} C_{\text{actual}} &= A - \sqrt{A^2 - B} \\ A &= L/4 - \pi(D+d)/8 \\ &= 1948/4 - \pi(550 + 300)/8 \\ A &= 153 \text{ mm} \\ B &= (D-d)^2/8 = (550 - 300)^2/8 \\ B &= 7813 \\ C_{\text{actual}} &= 153 + \sqrt{153^2 - 7813} \\ &= 277.88 \text{ mm} \\ C_{\text{actual}} &= 280 \text{ mm} \end{aligned}$$

2.2.3 Calculation of belt tension

$$\text{Power transmitted per belt} = (T_1 - T_2) v$$

$$2500 = (T_1 - T_2) \times 8.64$$

$$T_1 - T_2 = 290 \text{ N}$$

$$T_1 / T_2 = 3$$

$$T_2 = 290 \text{ N}$$

$$T_1 = 435 \text{ N}$$

Calculation of stress induced

$$\text{Stress induced } [\sigma] = \frac{\text{maximum tension}}{\text{Cross sectional Area}}$$

$$\text{Cross sectional Area of V Belt} = 140 \text{ mm}^2$$

$$[\sigma]_{\text{induced}} = 435 / 140$$

$$= 3.1 \text{ N/mm}^2 (> \text{ safe stress})$$

Therefore the design of safe

2.3 Design of gear

In speed reduction unit spur gear is used. In spur gear the teeth are straight and parallel to the shaft axis, Transmits power and motion between rotating two parallel shafts. The features of spur gear are easy to manufacturing, there are no axile force, relatively easy to produce high-quality gears, most common type of gear.

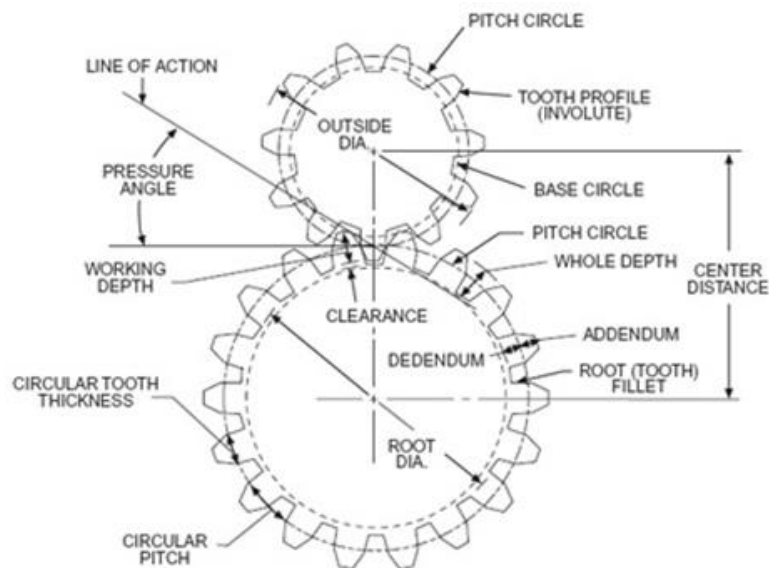


Fig.2.3.1. Spur gear drawing

Gear used in this mechanism is 20⁰ involute spur gear

Speed of gears in input shafts

- $N_1 = N_3 = 300$ rpm
- $N_2 = N_4 = 550/8 \approx 70$ rpm (1:8 speed reduction)

Transmission ratio (i)

$$i = N_1 / N_2$$

$$i = 300 / 70 = 4.3$$

Number of teeth

Assume number of teeth in Z_1 and $Z_3 = 18$

$$Z_2 = i \times Z_1 = 4.3 \times 18$$

$$Z_2 = 78$$

$$Z_2 = Z_4 = 78$$

2.3.1 Material selection

From design data book page number 8.4 ,for $i > 4$, C45 is taken material for both pinion and wheel

$$\text{Design twisting moment [Mt]} \quad [M_t] = M_t \times k_d \cdot K$$

$$k_d = \text{Dynamic load factor}$$

$$k = \text{load concentration factor}$$

$$k_d \cdot k = 1.3 \text{ (Assume for symmetric scheme)}$$

$$M_t = 97420 \times KW / n$$

$$= 97420 \times 2.5 / 300$$

$$M_t = 811.8 \text{ kgf.cm}$$

$$[M_t] = 811.8 \times 1.3$$

$$= 1055 \text{ kgf.cm}$$

$$\text{Design surface stress } [\sigma_c]$$

$$\text{Design surface compressive stress} \quad [\sigma_c] = C_R \cdot \text{HRC} \cdot K_{cl}$$

Rockwell Hardness,

$$\text{HRC} = 55 \text{ (for CI Grade 20, 25)}$$

$$C_R = 205$$

$$\text{Life factor for compressive stress, } K_{cl} = 1$$

$$[\sigma_c] = 205 * 1 * 55$$

$$= 14575 \text{ kgf/cm}^2$$

Center distance

$$a \geq (i + 1) \sqrt[3]{[(0.74 / [\sigma_c])^2 (E [M_t] / i X \psi)]}$$

$$\psi = 0.3 \text{ (from DDB Page no. 8.14)}$$

$$i = 4.3$$

$$E = 2.15 \times 10^6 \text{ kgf/cm}^2$$

Substituting the above values we get center distance $a = 20 \text{ cm}$

Module (m)

$$m = 1.26 \times \sqrt[3]{([M_t] / (y \times [\sigma_b] \psi_m \times Z_1))}$$

$$y = 0.377 \text{ (from DDB Page no. 8.18, for } Z = 18 \text{)}$$

$$\psi_m = 6 \text{ (from DDB Page no. 8.14)}$$

Substituting the above values we get module, $m = 0.3043 \text{ cm} = 0.4 \text{ cm}$ (standard module)

Checking for surface stress σ_c

$$\sigma_c = 0.74 (i+1)/a \sqrt{((i+1)/ib) E [M_t]}$$

$$\psi_m = b/m = 6$$

$$b = 6 \times 0.3 = 1.8 \text{ cm}$$

Substituting the above values we get $\sigma_c = 225 \text{ kgf/cm}^2 < [\sigma_c] = 14575 \text{ kgf/cm}^2$

Therefore design is safe.

Checking for bending stress σ_b

$$\begin{aligned} \text{Bending stress } \sigma_b &= [(i+1)/(a_m b y)] [M_t] \\ &= (4.3+1)/(20^2 \times 0.3 \times 1.8 \times 0.377) \\ \sigma_b &= 1373 \text{ kgf/cm}^2 < [\sigma_b] = 1840 \text{ kgf/cm}^2 \end{aligned}$$

Therefore design is safe

Dimensions Of Pinion And Gear

- Module $m = 0.4 \text{ cm} = 4 \text{ mm}$
- Center distance $a = 20 \text{ cm} = 200 \text{ mm}$
- Bottom clearance $c = 0.25 * m = 0.75 \text{ mm}$
- Tooth depth $h = 2.25 * m = 6.75 \text{ mm}$
- Pitch diameter $d_1 = m * z_1 = 72 \text{ mm}$, $d_2 = m * z_2 = 312 \text{ mm}$

2.4. Design of main hollow spindle

Pulley D

Power at pulley D is 2576 watts and its diameter is 550mm

Torque Transmitted

$$\begin{aligned} \text{Power } P &= (2\pi n T_D)/60 \\ T_D &= (60 * 2576)/(2\pi * 300) \end{aligned}$$

Therefore torque $T_D = 82 \text{ Nm}$

Total Load On Pulley D

Tension on tight side $T_1 = 447 \text{ N}$

Tension on slack side $T_2 = 149 \text{ N}$

Total load on pulley D is $W = T_1 + T_2 = 447 + 149$

$$W = 596 \text{ N}$$

Gear C

Diameter of gear C is 72mm and it has 20° involute angles. Since shaft is rotating at 300rpm as same as for pulley speed, its torque is 82N.m which is to be transmitted.

Normal Load In Gear C

Tangential force $F_t * R = T_D$, Radius $R = 36 \text{ mm}$

Tangential force $F_t = 2278 \text{ N}$

$$\begin{aligned} \text{Normal load} &= F_t / \cos 20^\circ = 2278 / \cos 20^\circ \\ &= 2424 \text{ N} \end{aligned}$$

Vertical Component Force

$$\begin{aligned} \text{Vertical component force} &= F_t * \cos 20^\circ \\ &= 2424 * \cos 20^\circ \\ &= 2278 \text{ N} \end{aligned}$$

Horizontal Component Force

$$\begin{aligned}\text{Horizontal component force} &= F_t \sin 20^\circ \\ &= 2424 \sin 20^\circ \\ &= 829 \text{ N}\end{aligned}$$

2.4.1. Gear E

Diameter of gear E is 312mm and it has 20° involute angle. Since shaft is rotating at 300rpm as same as for pulley speed, its torque is 82N.m which is to be transmitted.

NORMAL IN GEAR E

$$\text{Tangential force } F_t R = T_D, \text{ Radius } R=156 \text{ mm}$$

$$\text{Tangential force } F_t = 526 \text{ N}$$

$$\begin{aligned}\text{Normal load} &= F_t / \cos 20^\circ = 559 / \cos 20^\circ \\ &= 559 \text{ N}\end{aligned}$$

Vertical Component Force

$$\begin{aligned}\text{Vertical component force} &= F_t \cos 20^\circ \\ &= 559 \cos 20^\circ \\ &= 526 \text{ N}\end{aligned}$$

Horizontal Component Force

$$\begin{aligned}\text{Horizontal component force} &= F_t \sin 20^\circ \\ &= 559 \sin 20^\circ \\ &= 191 \text{ N}\end{aligned}$$

Bending Moment on Shaft

Vertical Loading

Reaction Forces For Vertical Loading

Taking moment about RBV

$$RAV * 200 - 2278 * 180 - 596 * 120 - 559 * 100 = 0$$

$$RAV = 2687 \text{ N}$$

$$RAV + RBV = 2278 + 596 + 559$$

$$RBV = 746 \text{ N}$$

Bending Moment For Vertical Loading

Bending moment at C

$$M_{CV} = RAV * 0.02 = 2687 * 0.02$$

$$M_{CV} = 53.7 \text{ Nm}$$

Bending moment at D

$$M_{DV} = RAV * 0.08 - C * 0.06 = 2687 * 0.08 - 2278 * 0.06$$

$$M_{DV} = 78.3 \text{ Nm}$$

Bending moment at E

$$M_{EV} = RAV * 0.1 - C * 0.08 - D * 0.02$$

$$M_{EV} = 74.5 \text{ Nm}$$

Horizontal loading

Reaction Force

Taking moment about RBH

$$RAH * 200 - 829 * 180 - 191 * 100 = 0$$

$$RAH = 842 \text{ N}$$

$$RAH+RBH=829+191=1020$$

$$RBH=178 \text{ N}$$

2.4.2 Bending moment for horizontal loading

Bending moment at C

$$M_{CH} = RAH * 0.02 = 842 * 0.02$$

$$M_{CH} = 16.8 \text{ Nm}$$

Bending moment at D

$$M_{DH} = RAH * 0.08 - C * 0.06 = 842 * 0.08 - 829 * 0.06$$

$$M_{DH} = 17.6 \text{ Nm}$$

Bending moment at E

$$M_{EH} = RAH * 0.1 - C * 0.08 - D * 0.02$$

$$M_{EH} = 17.8 \text{ Nm}$$

Maximum Bending Moment

Resultant bending moment at D

$$M_D = [(M_{DV})^2 + (M_{DH})^2]^{0.5}$$

$$= [(78.3)^2 + (17.6)^2]^{0.5}$$

$$M_D = 80.25 \text{ Nm}$$

Resultant bending moment at E

$$M_E = [(M_{EV})^2 + (M_{EH})^2]^{0.5}$$

$$= [(74.5)^2 + (17.8)^2]^{0.5} = 76.5 \text{ Nm}$$

From above it is clear that max bending moment occur at D

Therefore maximum bending moment $M_{max} = 80.25 \text{ Nm}$

2.4.3 Torque Equivalent

$$\text{Torque equivalent } T_{eq} = [(M_{DES})^2 + (T_{DES})^2]^{0.5}$$

Design bending moment

$$M_{DES} = K_b * M_{max}$$

Combined fatigue and shock factor for bending K_b is assumed to be 2

$$M_{DES} = 2 * 80.25$$

$$M_{DES} = 160.5 \text{ Nm}$$

Design torque

$$T_{DES} = K_t * T_{max}$$

Combined fatigue and shock factor for twisting K_t is assumed to be 1.5

$$T_{DES} = 1.5 * 82$$

$$T_{DES} = 123 \text{ Nm}$$

Torque equivalent

$$T_{eq} = [(M_{DES})^2 + (T_{DES})^2]^{0.5}$$

$$= [(160.5)^2 + (123)^2]^{0.5}$$

$$T_{eq} = 202 \text{ Nm}$$

2.4.4 Diameter of hollow spindle

$$T_{eq} = [(\pi/16) * \tau] [(D_o^4 - D_i^4) / D_o]$$

$$202 \cdot 10^3 = [(\pi/16) \cdot \tau] [(D_o^4 - D_i^4) / D_o]$$

Assume that the ratio of outside diameter to inside diameter is to be 1.35, i.e

$$D_o / D_i = 1.35$$

$$1.72 D_i^4 = (16 \cdot 202 \cdot 10^3) / (\pi \cdot 40)$$

Inside diameter $D_i = 24.66$ mm and

Outside diameter $D_o = 33.21$ mm

From DDB page no:7.20, standard diameter of shaft is taken as

Inside diameter $D_i = 25$ mm

Outside diameter $D_o = 35$ mm

3. Design of bearing

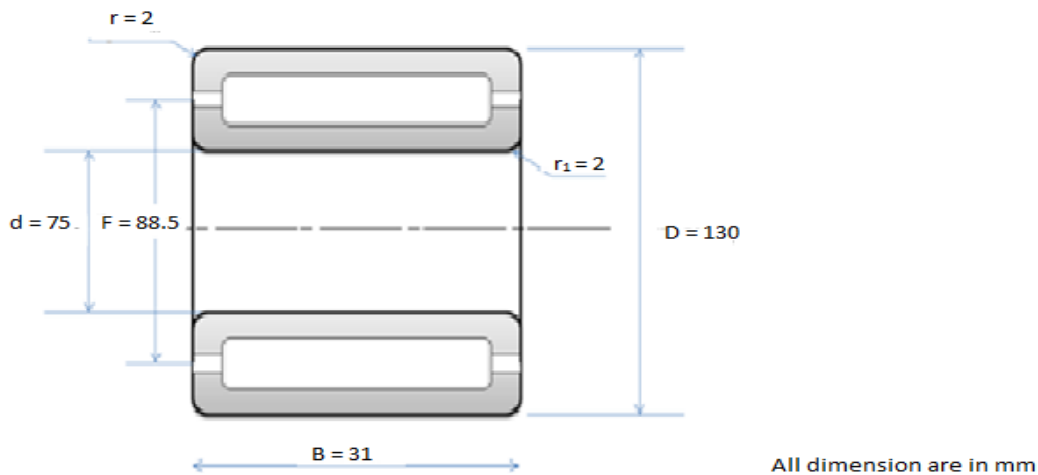


Fig3.1 Designed Bearing

Type of bearing used in back gear mechanism is *roller bearing*

From Nu 2.2 series for shaft diameter 60 mm

Diameter of bearing = 60 mm

Outer dia, $D = 110$ mm

Width, $B = 28$ mm

Outer corner radius, $r_2 = 2.5$ mm

Inner corner radius, $r_1 = 2$ mm

Static capacity, $C_o = 6200$ kgf

Dynamic capacity, $C = 7100$ kgf

$f = 73.5$ mm

Max. permissible feed = 6000 rpm

Equivalent bearing load (P)

$$\begin{aligned} C/P &= 4.5 \\ P &= C/4.5 \\ &= 7100/4.5 \\ P &= 1578 \text{ kgf} \end{aligned}$$

Life of bearing

$$\begin{aligned} L &= (C/P)^{10/3} \\ &= (7100/1578)^{10/3} \\ L &= 150.14 \text{ mm} \\ &= (150.14 \times 10^5) / 60 \times \text{rpm} \\ &= (150.14 \times 10^5) / 60 \times 300 \\ L &= 8358 \text{ hrs.} \end{aligned}$$

Comparing in graph from DDB Page no. 4.7

For 300 rpm and C/P = 4.5,

L = 8500 hrs. , which is approximately equal to calculated life time

4. RESULTS AND DISCUSSIONS

4.1. DESIGN OF BELT DRIVE

B Section is selected for the given power of 7 kW,

- Nominal top width $w = 17 \text{ mm}$
- Nominal thickness $T = 11 \text{ mm}$
- Nominal pitch length $L = 2888 \text{ mm}$
- Arc of contact angle $\theta = 155^\circ$
- Maximum power capacity $\text{kW} = 5.4 \text{ KW}$
- Number of belt $n_b = 3$
- Actual Center Distance $C_{\text{actual}} = 755 \text{ mm}$

4.2. DESIGN OF GEAR

The gear used are 20° full depth involute spur gear

- Number of teeth in $Z_1 = 20, Z_2 = 80$
- Module $m = 0.4 \text{ cm} = 4 \text{ mm}$
- Center distance $a = 20 \text{ cm} = 200 \text{ mm}$
- Bottom clearance $c = 0.25 * m = 0.75 \text{ mm}$
- Tooth depth $h = 2.25 * m = 6.75 \text{ mm}$
- Pitch diameter $d_1 = m \times Z_1 = 80 \text{ mm}$
 $d_2 = m \times Z_2 = 320 \text{ mm}$

4.3. DESIGN OF INTERMEDIATSHAFT

Standard diameter of hollow spindle is

- Diameter $d = 75 \text{ mm}$

4.4. DESIGN OF BEARING

- Diameter of bearing $d = 75 \text{ mm}$
- Outer diameter $D = 130 \text{ mm}$
- Width $B = 31 \text{ mm}$
- Outer corner radius, $r_2 = 2.5 \text{ mm}$
- Inner corner radius, $r_1 = 2.5 \text{ mm}$

- | | | |
|----|--------------------------|------------------|
| f. | Static capacity, | $C_o = 8650$ kgf |
| g. | Dynamic capacity, | $C = 9800$ kgf |
| h. | Distance between rollers | $F = 88.5$ mm |

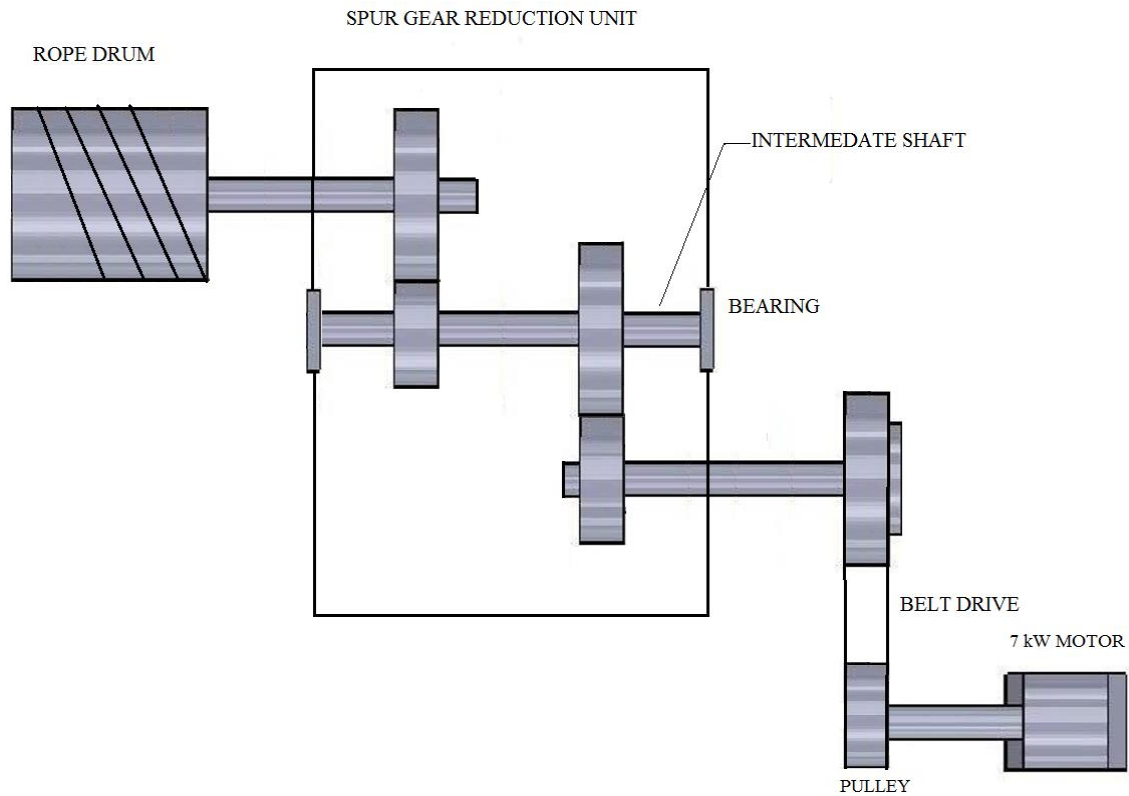


Fig 4.1 Layout Of Drive Arrangement

5. CONCLUSION

The detailed study of back gear mechanism about its working and its layout is made. Also discussed about the design procedure involved in design of back gear mechanism in lathe. The design procedure include the following design calculation

1. DESIGN OF BELT DRIVE
2. DESIGN OF GEAR
3. DESIGN OF MAIN HOLLOW SPINDLE
4. DESIGN OF LAY SHAFT
5. DESIGN OF BEARING

The design calculations made are compared with its allowable stress values which ensure the safe design for back gear mechanism.

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