

Solar power Estimate Using Different Empirical Constant

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ABSTRACT

Solar radiation data an important role in solar energy. Theses radiation data are not available for all location of interest due to absence of meteorological station, especially in remote locations. This study evaluates different empirical models on Angstrom Present model to estimate global solar radiation using specific connection based on sunshine hours. We have estimated the value of monthly global solar radiation for Chennai. The values of monthly average global solar radiation are calculated using the expression constants in the models.(linear, quadratic, cubic, log, exponent) all the regression models investigated, validated and compared. The calculated data from these models is compared with the data provided by MNRE. The calculated and measured data are simulated using MAT-LAB, on comparison. It was observed that the cubic models are overall more accurate for calculating the global solar radiation for the Chennai region. The regression co-efficient is used to find the curve fitting technique. The present works will help to advance the state of knowledge of global solar radiation to the estimation of solar global radiation (SGR).

Key Words: curve fitting tool, Daily global solar radiation, Empirical models, Sunshine hours, Validation, MAT-LAB.

1 INTRODUCTION

The earth and its atmosphere depend ultimately on the sun for its energy supply. The radiant energy from the sun covers the entire electromagnetic spectrum. The atmospheric interference restricts this spectrum to 290nm to 300nm which is called "Solar radiation" energy. From solar radiation can be derived by thermal conversion where in the heat generated due to irradiation is used to operate a system and by direct conversion into electrical energy. The accurate information of the solar radiation intensity at a given location is essential to the development of solar energy based projects and in the long term evaluation of the solar energy conversion systems performance [1]. This information is used in the design of a project. Furthermore monthly mean daily data are needed for the estimation of long term solar systems performances. Furthermore daily global solar radiation models required for engineering design and planning projects [2,3]. Solar radiation which arrives to earth surface for every year is 160 times the world's proven fossil fuel and reserves [4]. A global study has been made on the global solar radiation models are available the study carried out an estimation of the monthly average daily global solar radiation on horizontal surface [5] among several empirical models which have been used to calculate global solar radiation the most commonly used parameters in sunshine hours [6].The empirical models has been used to calculate global solar radiation are usually based on some factors as shown in table (1)[7]. Since the solar radiation reading the earth's surface depends upon climate condition of the place. A study of solar radiation under local climatic conditions of the place is necessary. This knowledge of local

solar radiation is essential for the proper design of buildings energy systems, solar energy systems and a good evaluation of thermal environment within the buildings [8-11]. It is measured in terms of sunshine duration. One way of solving this is using appropriate correlations which are empirically established that can be used to estimate global solar radiation from more readily available metrological parameters such as sunshine hours. Several empirical models have been developed to calculate solar radiation from meteorological, geographical, climatologically parameters such as relative humidity, ambient temperature, soil temperature, number of rainy days and evaporation [12-18]. In addition, other empirical models have been developed to calculate solar radiation from sunshine hours [19-22]. The most commonly used parameters for estimating global solar radiation are sunshine duration among various correlations. The modified variations of [23] model who proposed a linear relationship between the ratio of corresponding value on a clear sky day and the ratio of average daily sunshine duration to the maximum possible sunshine duration and its derivatives have been widely used. Empirical models which have been used to calculate global radiation are usually on some factors as shown in table [1], [23]. The Solar radiation data computed based on measured metrological data computed data. The average daily global radiation on horizontal surface it, for a location is now possible of sunshine hours five different models have been selected from different previous studies for estimating daily global solar radiation. All models have been proposed for estimating for monthly mean daily global solar radiation, H-based on the Angstrom-Prescott model [24].

TABLE 1: CLASSIFICATION OF PARAMETERS USED TO CALCULATE SOLAR RADIATION (GSR)

Classification	Parameter
Meteorological factors	Extraterrestrial solar radiation, sunshine duration, temperature, precipitation, relative humidity, effects of cloudiness, soil temperature, evaporation, reflection of the
Geometrical factors	Azimuth angle of the surface, tilt angle of the surface, sun elevation angle, sun azimuth angle.
Physical factors	Scattering of dust and other atmospheric constituents such as O ₂ , N ₂ , Co ₂ and O
Geographical factors	Latitude, Longitude and elevation of the site
Astronomical factors	Solar constant, earth – sun distance, declination and hour angle

2 NEEDED FOR SOLAR RADIATION DATA

A whole array of application via, thermal conversion, photovoltaic conversion, photochemical utilization, biomass of buildings, detoxication etc is becoming apparently viable and enhances the societies energy management planning and hence its efficient applications. The economics of these technologies depend on the efficiency of the utilizing processes. So that the operating costs are comparable if not cheaper. With the present day processes based on conventional fossilized energy utilization. Thus to design operating systems which will have the highest achievable efficiency under comparable costs. The reliable database on different aspects of solar radiation energy is essential. The more accurately the solar resources are known. The better becomes the system design the radiation energy available at a location changes throughout the day and year due to varying weather patterns by knowing the variability storage systems can be designed and used optimally. Solar radiation data also help to determine the best geographic location for utilization as it will have a direct influence on the design of the systems. Photovoltaic and photochemical conversions need spectral distribution over space and

time, location, climate and atmospheric conditions have strong influence on the spectral distribution of solar irradiance.

TABLE 2: THE REGRESSION MODELS PROPOSED IN LITERATURE

Model No	Regression Equation	Model Type
1	$H/H_0 = a + b (s/S_0)$	Linear
2	$H/H_0 = a + b (s/S_0) + c(s/S_0)^2$	Quadratic
3	$H/H_0 = a + b (s/S_0) + c(s/S_0)^2 + d(s/S_0)^3$	Cubic
4	$H/H_0 = a + b \log(s/S_0)$	Logarithmic
5	$H/H_0 = a + b \exp(s/S_0)$	Exponential

3 CALCULATION PROCEDURES

Many different models have been found in the literature such as linear, quadratic, cubic, logarithmic, exponential regressing model to estimate on a horizontal surface from observed sunshine duration and calculate extraterrestrial radiation and maximum possible sunshine duration. In this study model have been investigated and validity of this model has been made. The Angstrom Prescott model [24] that examines the linear correlation between clearness index (H/H₀) and sunshine duration ratio (S/S₀) is most commonly used model. The equation used in this model is,

$$H/H_0 = a + b (S/S_0) \tag{1}$$

Where H is monthly average daily global radiation on a horizontal surface,
 H₀ is a extraterrestrial radiation on a horizontal surface
 S is a monthly average daily sunshine duration
 S₀ is a monthly average maximum possible daily sunshine duration and
 a, b are Angstrom coefficient (also called regression coefficient)

$$H/H_0 = a + b (S/S_0) + C (S/S_0)^2 \tag{2}$$

The quadratic model is proposed by Akinolgu and Ecevit .et.al [25] and the related equation isThe cubic model is proposed by Bahel et .al [26]. And the related equation is

$$H/H_0 = a + b (S/S_0) + C (S/S_0)^2 + d (S/S_0)^3 \tag{3}$$

The logarithmic model is proposed by D.B Ampratoumandet.al [27] and the related equations is

$$H/H_0 = a + b \log (S/S_0) \tag{4}$$

The exponential model is proposed by J. Almorexet.al [28] and related equation is

$$H/H_0 = a + b \exp (S/S_0) \tag{5}$$

The monthly average daily extraterrestrial radiation on a horizontal surface can be calculated by following equation [29]

$$H_0 = 24 \cdot 3600 / \pi \cdot I_{sc} \cdot (1 + 0.003 \cos 360 \cdot n + (284 + d / 365)) (\cos \varnothing \cos s \sin w_s \sin \pi (\sin w_s / 180)) \tag{6}$$

Where I_c is the solar constant (1367 W/m²), ∅ is the latitude of the location , s is the sun declination and W_s is the sunset hour angel for a given month and D or N is the no of days of the year starting from 1st of January. Declination sunset hour angel and day length can be computed by the following equation [30, 31].

$$s = 23.45 \sin [360 + (284 + (d/365))] \quad (7)$$

Where d is the day of the year 365

$$W_s = \cos^{-1} (-\tan \phi \tan s) \quad (8)$$

$$S_0 = 2/15 W_s \quad (9)$$

Further five different models have been selected from different previous studies for estimating daily global solar radiation. All models having proposed for estimating the monthly mean daily global radiation. H based on the Angstrom Prescott model, extraterrestrial radiation on a horizontal surface sin daily period where calculated numerically for each month using declination angel, latitude and sunset hour angel from the calculation procedure using the equation [32, 33, 34]. Then we develop equation to estimate H/H₀ for each month by applying regression analyze to the parameter S/S₀ based on the model equation, five model equation for each month where formed. The values of monthly average of daily solar radiation estimated for each month. The corresponding measured value are compared with the estimated values using the above five models for each month.

3.1 STATISTICAL ROUTINE

Each month was evaluated on the basis of the statistical error tests, (i.e. the mean bias error (MBE), mean percentage error (MPE), root mean square error (RMSE), and coefficient of determination, R^2). The equations were also tested whether they are statistically significant using t -statistics.

3.1.1 THE MEAN BIAS ERROR

$$MBE = \frac{1}{N} \sum_{i=1}^N (C_i - M_i) \quad (10)$$

where C_i and M_i are the forecast and actual values of solar radiation being forecast respectively, and N is the number of observations. This test provides information on long-term performance. A low MBE value is desired. A mean error value of zero can mean the method forecasts the actual values perfectly or that the positive and negative errors cancel each other out. So, one drawback of this test is that it tends to understate the error in all cases.

3.1.2 MEAN PERCENTAGE ERROR

$$MPE(\%) = \frac{100}{N} \sum_{i=1}^N \frac{C_i - M_i}{M_i} \quad (11)$$

MPE quantifies the schematic component of the normalized difference for individual observations. It is subjected to the averaging of the positive and negative errors. A percentage error between -10% and +10% is considered acceptable.

3.1.3 THE ROOT MEAN SQUARE ERROR

$$RMSE = \left[\frac{1}{N} \sum_{i=1}^N (C_i - M_i)^2 \right]^{\frac{1}{2}} \quad (12)$$

The value of RMSE is always positive, representing zero in the ideal case. The normalized roots mean performance of the correlations by allowing a term by term comparison of the actual deviation between the

predicted and measured values. The smaller the value, the better is the model's performance.

3.1.4 THE COEFFICIENT OF DETERMINATION, R²

The coefficient of determination, *R* give some information about the goodness of fit of a model. In regression, the *R*² coefficient of determination is a statistical measure of how well the regression line approximates the real data points.

$$3. \quad t = \frac{(N - 1)(MBE)^2}{(RMSE)^2 - (MBE)^2} \quad (12)$$

T-statistics is an indicator of adjustment between calculated and measured data allowing the data to be compared. It can be used to induce whether or not data measurements are statistically significant at a particular confidence level.

4 RESULTS AND DISCUSSION

The accuracy of five model equations were determined using data measured at Chennai city from. The regression coefficients *a*, *b*, *c* and *d* are given for all five models for each month are shown in Tables 4.1.

TABLE 4.1: REGRESSION COEFFICIENT FOR CHENNAI CITY

Model Type	Model Number	A	b	c	d
linear	1	0.059	0.631	-	-
log	2	0.681	0.503	-	-
Power	3	0.689	0.893	-	-
Quadratic	4	0.112	0.497	0.083	-
$t = \frac{(N - 1)(MBE)^2}{(RMSE)^2 - (MBE)^2}$		1.193	-3.642	5.326	-2.196

The regression coefficients were obtained using curve fitting tool in MATLAB. The values of the mean daily global solar radiation estimated using the above five models were compared with the corresponding measured values. Statistical test MBE, MPE, RMSE, R and *t*-test were determined for all five model equations for each month of the year. The applicability of the proposed correlations in predicting the daily mean global solar radiation is tested by estimating values for Chennai city used in the analysis. Estimated values for the five models with measured data for the months January to December shown in Tables 4.2.

TABLE 4.2: COMPARISON BETWEEN MEASURED AND ESTIMATED VALUES (H) OF THE CORRELATION EQUATION (CHENNAI CITY)

Statistical parameters	Model 1	Model 2	Model 3	Model 4	Model 5
MBE	-0.0007	0.0002	0.0001	0.0001	0.0000
MPE	-0.1189	0.0383	0.0171	0.0179	0.0074
RMSE	0.0024	0.0015	0.0013	0.0014	0.0014
R ²	0.9956	0.9910	0.9956	0.9956	0.9966
t-stat	0.9574	0.9574	0.9574	0.9574	0.9576

It was found that the measured data for January, -0.1189, low RMSE value of 0.0024, November. All the values are always equal to 0.9956, different models give similar values. These results are (above 0.95) indicate that the measured data is for predicting the daily altitude as radiation using the model respectively.

Month	Day	Measured (MJ/m ²)	Model 1 (MJ/m ²)	Model 2 (MJ/m ²)	Model 3 (MJ/m ²)	Model 4 (MJ/m ²)	Model 5 (MJ/m ²)
Jan	1	17.56	17.39	17.81	17.68	17.65	17.65
Feb	2	21.06	20.39	20.75	20.70	20.70	20.72
Mar	2	23.46	23.32	23.56	23.63	23.68	23.60
Apr	2	24.13	23.85	24.18	24.19	24.21	24.19
May	2	22.86	22.33	22.82	22.68	22.66	22.69
Jun	2	21.41	21.19	21.71	21.54	21.51	21.50
Jul	1	19.62	19.65	20.12	19.99	19.97	19.90
Aug	1	19.05	18.55	18.90	18.89	18.90	18.85
Sep	2	20.07	19.64	20.13	19.98	19.95	19.90
Oct	1	17.41	17.12	17.48	17.42	17.43	17.36
Nov	1	14.61	14.43	14.55	14.69	14.75	14.80
Dec	1	14.69	14.64	14.93	14.90	14.91	14.86

Model 5

Month	Measured (MJ/m ²)	Model 1 (MJ/m ²)	Model 2 (MJ/m ²)	Model 3 (MJ/m ²)	Model 4 (MJ/m ²)	Model 5 (MJ/m ²)
Jan	17.56	17.39	17.81	17.68	17.65	17.65
Feb	21.06	20.39	20.75	20.70	20.70	20.72
Mar	23.46	23.32	23.56	23.63	23.68	23.60
Apr	24.13	23.85	24.18	24.19	24.21	24.19
May	22.86	22.33	22.82	22.68	22.66	22.69
Jun	21.41	21.19	21.71	21.54	21.51	21.50
Jul	19.62	19.65	20.12	19.99	19.97	19.90
Aug	19.05	18.55	18.90	18.89	18.90	18.85
Sep	20.07	19.64	20.13	19.98	19.95	19.90
Oct	17.41	17.12	17.48	17.42	17.43	17.36
Nov	14.61	14.43	14.55	14.69	14.75	14.80
Dec	14.69	14.64	14.93	14.90	14.91	14.86

Month	Measured (MJ/m ²)	Model 1 (MJ/m ²)	Model 2 (MJ/m ²)	Model 3 (MJ/m ²)	Model 4 (MJ/m ²)	Model 5 (MJ/m ²)
Jan	17.56	17.39	17.81	17.68	17.65	17.65
Feb	21.06					
Mar	23.46					
Apr	24.13					
May	22.86					
Jun	21.41					
Jul	19.62					
Aug	19.05					
Sep	20.07					
Oct	17.41	17.12	17.48	17.42	17.43	17.36
Nov	14.61	14.43	14.55	14.69	14.75	14.80
Dec	14.69	14.64	14.93	14.90	14.91	14.86

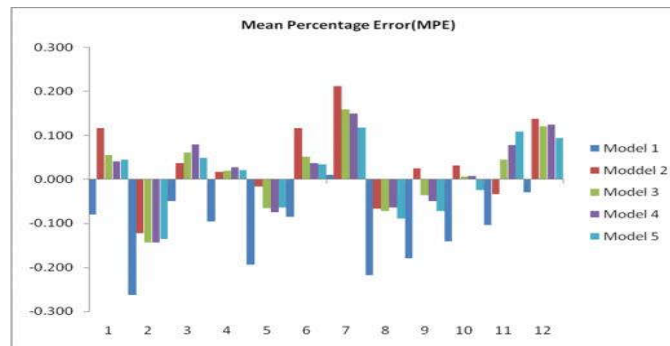
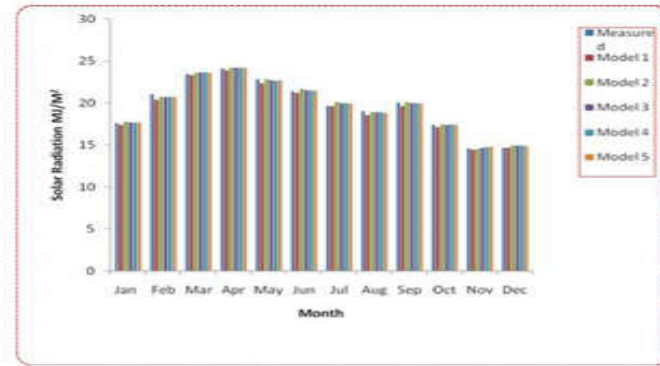


Fig. 4.2 Month Vs Mean Vias Error

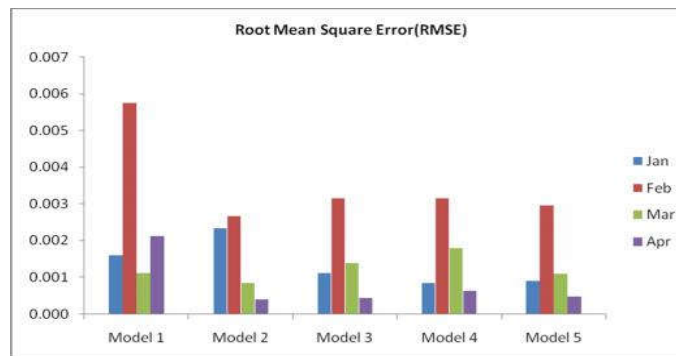


Fig 4.3. Model Vs Root Mean Square Error

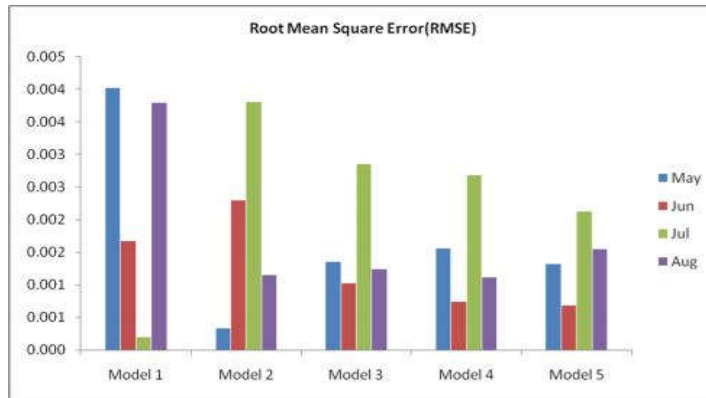


Fig. 4.4 Model Vs Month

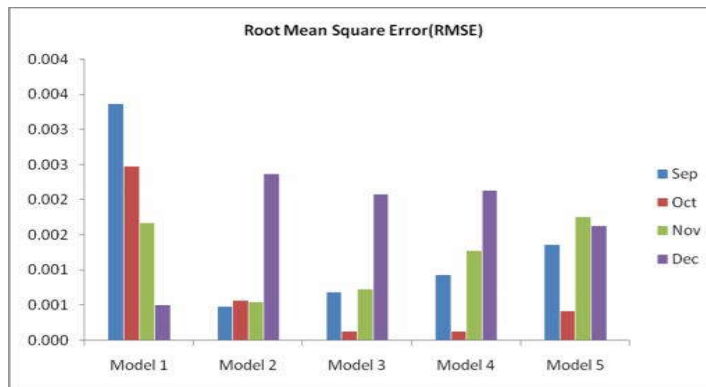


Fig 4.5. Model Vs Root Mean Square Error

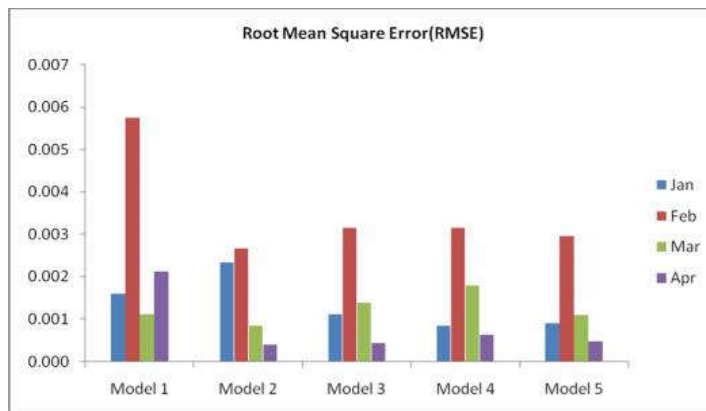


Fig 4.6. Model Vs Root Mean Square Error

V CONCLUSIONS

The main objective of this paper is to calculate the global solar radiation from sunshine duration. The calculated results are compared with the measured data available at Chennai, and calculated value found to be acceptable within the limited error range.

- ❖ Based on the radiation data and sunshine hours data were provided by IMD.
- ❖ The linear, quadratic, cubic, logarithmic and power equations are generated and also investigation on regression models.
- ❖ According to the statistical test results are obtained and graphs were plotted the cubic models are accurate than the other regression models.
- ❖ These regression models give good agreement between the measured and computed values of solar global radiation. Although all five developed models are able to found good accuracy the correlation of solar radiation and sunshine data. (Cubic) gives the more accuracy fit for the Chennai region
- ❖ The percentage of error between measured and calculated results for Chennai region lies within the range of 10% to 15% models can be used for the validation of local solar radiation data, which is essential for the design of infrastructure, solar power plants etc., for the developing country.

REFERENCES

- [1] A.M. Muzathik, W.B.W. Nik, *Daily global solar radiation estimate based on sunshine hours*, Energy Converse Manage 2011;75:80-6.
- [2] Genwa KR, Sagar CP, *Solar energy conversion and storage in photogalvanic cell*. Energy Convers Manage 2013;66:121-6.
- [3] Tarhan S, Sari A. *Model selection for global and diffuse radiation over the Central BlackSea CBS) region of Turkey*. Energy Converse Manage 2005;46:605-13.
- [4] Ultanır MO. 21. Yuzyilin Esiginde Gunes Enerjisi. Bilim ve Teknik, *Energy Efficiency* 1996;340:50-5.
- [5] Bakirci K. *Models of solar radiation with hours of bright sunshine: A review*. Renewable Sust Energy Rev 2009;13:2580-8.
- [6] Zhao N, Zeng X, Han S. *Solar radiation estimation using sunshine hour and air pollution index in China*. Energy Convers Manage 2013;76:846-51.
- [7] Besharat F, Dehghan AA, Faghih AR. *Empirical models for estimating global solar radiation: a review and case study*. Renewable Sust Energy Rev 2013;21:798-821.
- [8] Lu Z, Piedrahita RH, Neto CDS. *Generation of daily and hourly solar radiation values for modeling water quality in aquaculture ponds*. Transactions of the ASAE 1998;41(6):1853-9.(8).

- [9] Machler MA, Iqbal M. *A modification of the ASHRAE clear-sky irradiation model*. ASARE Transactions 1985;9(1a):106-115.
- [10] Cartwright TJ. Here comes the sun: *solar energy from a flat-plate collector*. In: *Modelling the world in a spreadsheet- environmental simulation on a micro-computer*. London: The Johns Hopkins University Press;1993, 121-44.9(10)
- [11] Trujillo JHS. *Solar performance and shadow behavior in buildings-case study with computer modeling of a building in Loranca, Spain*. Building and Environment 1998;33(2-3):117-30.(11).
- [12] M. Yorukoglu and A.N. Celik, *A critical review on the estimation of daily global solar radiation from sunshine duration*, Energy Conversion and Management, vol.47, no.15, pp. 2441-2450, 2006.
- [13] T.T. Chow, A.L.S. Chan, K.F. Fong and Z. Lin, *Some perceptions on typical weather year-from the observations of Hong Kong and Macau*, Solar Energy, 2006, vol. 80, pp. 459-467.
- [14] M. El-Metwally, *Sunshine and global solar radiation estimation at different sites in Egypt*, Journal of Atmospheric and Solar-Terrestrial Physics, vol. 67, no. 14, pp. 1331-1342, 2005.
- [15] S. Rehman and T.O. Halawani, *Global solar radiation estimation*, Renewable Energy, vol. 12, no. 4, pp. 369-385, 1997.
- [16] I.T. Togrul and E. Onat, *A study for estimating solar radiation in Elazığ using geographical and meteorological data*, Energy Conversion and Management, vol. 40, pp.1577-1584, 1999.
- [17] N.A. Elagib and M.G. Mansell, *New approaches for estimating global solar radiation across Sudan*, Energy Conversion and Management, vol. 41, no.5, pp. 419- 434, 2000.
- [18] C. Ertekin and O.Yaldiz, *Comparison of some existing models for estimating global solar radiation for Antalya (Turkey)*, Energy Conversion and Management, vol. 41, no. 4, pp. :311-330, 2000.
- [19] K. Bakirci, *Correlations for estimation of daily global solar radiation with hours of bright sunshine in Turkey*, Energy, vol. 34, pp. 485-501, 2009.
- [20] M.Koussa, A.Malek and M. Haddadi, *Statistical comparison of monthly mean hourly and daily diffuse and global solar irradiation models and a Simulink program development for various Algerian climates*, Energy Conversion and Management, vol. 50, pp. 1227-1235, 2009.
- [21] H.Bulut and O.Buyukalaca, *Simple model for the generation of daily global solar-radiation data in Turkey*, Applied Energy, vol. 84, pp. 477-491, 2007.
- [22] B.G.Akinoglu and A. Ecevit, *Construction of a quadratic model using modified Angstrom coefficients to estimate global solar radiation*, Solar Energy, vol. 45, pp. 85-92, 1990.
- [23] Besharat F, Dehghan AA, Faghih AR. *Empirical models for estimating global solar radiation: A review and case study*. Renewable Energy Rev 2013; 21:798-821.

- [24] A. Angstrom, Qr J R Meteor Soc, *Solar and atmospheric radiation*, vol. 50, pp. 121, 1924.
- [25] Ulgen K, Hepbasli A. Solar radiation models. Part 2: *Comparison and developing new models*. Energy Sources 2004; 26:52130.
- [26] Almorox J, Hontoria C. *Global solar radiation estimation using sunshine duration in Spain*. Energy Converts Manage 2004; 45:1529–35.
- [27] D.B Ampratwumand A.S.S.Dorvlo, *Estimation of solar radiation from the number of sunshine hours*, Applied Energy, vol. 63, pp. 161–167, 1999.
- [28] J.Almorox, M. Benito and C. Hontoria, *Estimation of monthly Angstrom, Prescott equation coefficients from measured daily data in Toledo, Spain*, Renewable Energy, vol.30, pp. 931–936, 2005.
- [29] Ahmad F, Ulfat I. *Empirical models for the correlation of monthly average daily global solar radiation with hours of sunshine on a horizontal surface at Karachi, Pakistan*. Turkish J Phys 2004; 28:301–7.
- [30] Tiris M, Tiris Ç, Türe I_E. *Correlations of monthly-average daily global, diffuse and beam radiations with hours of bright sunshine in Gebze, Turkey*. Energy Convers Manage 1996; 37:1417–21.
- [31] Rehman S, *Solar radiation over Saudi Arabia and comparisons with empirical models*. Energy 1998; 23:1077–82.
- [32]. N.A. Elagib and M.G.Mansell, *New approaches for estimating global solar radiation across Sudan*, Energy Conversion and Management, vol. 41, no.5, pp. 419- 434, 2000.
- [33]. C. Ertekin and O.Yaldiz, *Comparison of some existing models for estimating global solar radiation for Antalya* Energy Conversion and Management, vol. 41, no. 4, pp.311-330,2000.
- [34]. K. Bakirci, *Correlations for estimation of daily global solar radiation with hours of bright sunshine in Turkey*, Energy, vo34, pp. 485-501,2009.